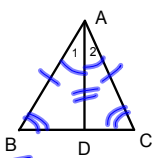


Warmup!

Given:  $\overline{AD}$  bisects  $\angle BAC$   
 $\overline{AB} \cong \overline{AC}$

Prove:  $\angle B \cong \angle C$



<p>S.</p> <ol style="list-style-type: none"> <li>①</li> <li>② <math>\angle 1 \cong \angle 2</math></li> <li>③ <math>\overline{AD} \cong \overline{AD}</math></li> <li>④ <math>\triangle BAD \cong \triangle CAD</math></li> <li>⑤ <math>\angle B \cong \angle C</math></li> </ol>	<p>R.</p> <ol style="list-style-type: none"> <li>① Given</li> <li>② def of <math>\angle</math> Bis.</li> <li>③ Refl.</li> <li>④ SAS</li> <li>⑤ CPCTC</li> </ol>
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## 4.7 Use Isosceles and Equilateral Triangles

 $\triangle ABC$  is isosceles

$\overline{AB} \cong \overline{AC}$

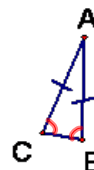


$\angle A$  is the vertex angle  
 $\angle B$  and  $\angle C$  are the base angles

**B.A.T.**

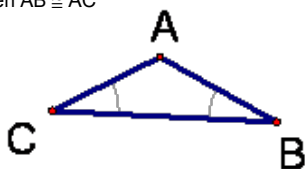
Base Angles Theorem-(Theorem 4.7) If 2 sides of a  $\triangle$  are  $\cong$ , then the angles opposite those sides are  $\cong$ .

Since  $\overline{AB} \cong \overline{AC}$ , then  $\angle C \cong \angle B$

**Conv. BAT**

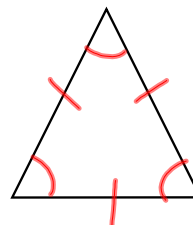
The Converse of the Base Angles Theorem-(Theorem 4.8) If 2 angles of a  $\triangle$  are  $\cong$ , then the sides opposite those angles are  $\cong$ .

Since  $\angle C \cong \angle B$ , then  $\overline{AB} \cong \overline{AC}$



Corollary -If a  $\triangle$  is equilateral, then it is equiangular

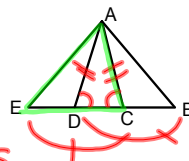
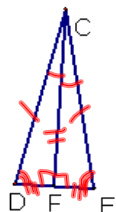
Corollary -If a  $\triangle$  is equiangular, then it is equilateral



\*\*\*\*\*The altitude of an isosceles  $\triangle$  is  $\perp$  to the base at its midpoint.

If  $\overline{CF}$  is the altitude from the vertex angle, then  $DF = FE$  and  $m\angle CFE = 90^\circ$

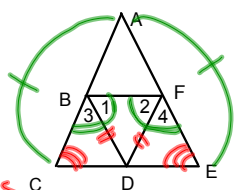
Why?  $\triangle DFC \cong \triangle EFC$  by HL



Given:  $\overline{EC} \cong \overline{DB}$ ;  $\angle ACD \cong \angle ADC$

Prove:  $\triangle ECA \cong \triangle BDA$

S.	R.
①	① Given
② $\overline{AD} \cong \overline{AE}$	② Conv. B.A.T
③ $\triangle ECA \cong \triangle BDA$	③ SAS



Given:  $\overline{AC} \cong \overline{AE}$ ;  $\angle 1 \cong \angle 2$ ;  $\angle 3 \cong \angle 4$

Prove:  $\triangle BCD \cong \triangle FED$

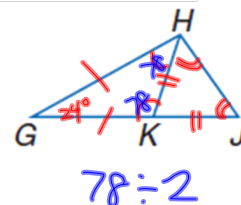
S.	R.
①	① Given
② $\angle C \cong \angle E$	② B.A.T.
③ $\overline{BD} \cong \overline{FE}$	③ Conv. B.A.T.
④ $\triangle BCD \cong \triangle FED$	④ AAS

No to scale!

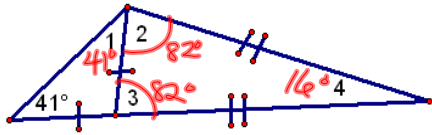
In the figure,  $\overline{GK} \cong \overline{GH}$  and  $\overline{HK} \cong \overline{KJ}$ .

$$m\angle G = 24$$

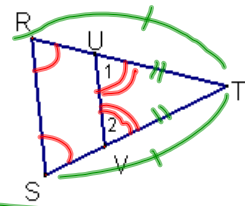
$$m\angle J = 39^\circ$$



Find the measures of the numbered angles.



Given:  $\angle R \cong \angle S$   
 $\angle 2 \cong \angle 1$   
 Prove:  $\overline{RU} \cong \overline{SV}$

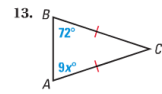
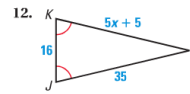
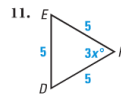


- |  |   |
|--|---|
| <p>S.</p> <ol style="list-style-type: none"> <li>①</li> <li>② <math>\overline{RU} \cong \overline{SV}</math><br/><math>\overline{UT} \cong \overline{VT}</math></li> <li>③ <math>RT = ST</math> <math>UT = VT</math></li> <li>④ <math>RT = RU + UT</math><br/><math>ST = SV + VT</math></li> <li>⑤ <math>RU + UT = SV + VT</math></li> <li>⑥ <math>RU = SV</math></li> <li>⑦ <math>\overline{RU} \cong \overline{SV}</math></li> </ol> | <p>R.</p> <ol style="list-style-type: none"> <li>① Given</li> <li>② Conv. BAT</li> <li>③ def of <math>\cong</math></li> <li>④ SAP</li> <li>⑤ Subst.</li> <li>⑥ Subtr.</li> <li>⑦ def of <math>\cong</math></li> </ol> |
|--|---|

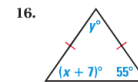
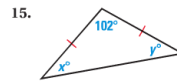
HW

p267-268 #s 11-13, 15-17,  
 20-22, 32, 33, plus 2  
 proofs sent out in  
 classroom

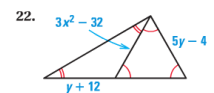
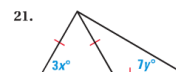
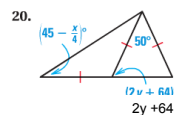
**11. ALGEBRA** Find the value of  $x$ .



**15. ALGEBRA** Find the values of  $x$  and  $y$ .



**16. ALGEBRA** Find the values of  $x$  and  $y$ , if possible. Explain your reasoning.



**32** ALGEBRA Find the value(s) of the variable(s). *Explain* your reasoning.

